

## A Note on Dedekind Modules

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### EXTENDED ABSTRACT :

This work studies relations among a Dedekind module, an HNP (hereditary Noetherian and prime) module, and an order of a module. Then, the obtained properties will be employed to investigate a relation between a Dedekind algebra and a strongly-coprime cohereditary coalgebra.

McConnell and Robson (1987) documented the following interrelation; a ring  $R$  is a Dedekind prime ring if and only if it is an HNP ring and a maximal order. In this work we extend this result concerning Dedekind modules.

The concept of a Dedekind module was introduced and studied in Naoum and Al-Alwan (1996) as a generalization of the concept of a Dedekind ring. The most of those results dealt with a class of multiplicative modules and faithful modules. The concept of an order of a module will be introduced as a generalization of the concept of a ring.

Let  $R$  be an order in  $Q$ . An  $R$ -module  $N$  is said to be an order of the  $R$ -module  $M$  if  $N$  is an  $R$ -submodule of  $M$  such that for all  $m \in M$ ,  $m = ns^{-1}$  for some  $n \in N$  and  $s \in S$ .

Studying those results and follows other works and analysis results, it was observed that every Dedekind projective  $R$ -module is HNP and If  $R$  is an integral domain and  $M$  be a Dedekind projective torsion free  $R$ -module than  $M$  is an HNP and a maximal order. Further, we apply those result to algebra and coalgebra notion. Particularly, if  $R$  is self injective and cogenerator and  $C$  is Dedekind  $R$ -algebra, then  $C$  is strongly coprime cohereditary  $R$ -coalgebra.